

NUHEP-TH-96-5

# COMPARATIVE STUDY OF THE HADRONIC PRODUCTION OF $B_c$ MESONS\*

ROBERT J. OAKES

*Department of Physics and Astronomy,**Northwestern University, Evanston, IL 60208, USA*

## Abstract

The full order  $\alpha_s^4$  perturbative QCD calculation of the production of  $B_c$  mesons at the Tevatron is compared with the fragmentation approximation. The non-fragmentation diagrams, in which two or more quarks and/or gluons can simultaneously be nearly on-shell, are important unless  $P_T \gg M_{B_c}$ .

## I. INTRODUCTION

Hadronic production of  $B_c$  and  $B_c^*$  mesons is of considerable, current interest. At hadronic colliders, the dominant subprocess is  $g + g \rightarrow B_c(B_c^*) + b + \bar{c}$  and 36 Feynman diagrams contribute in the lowest order,  $\alpha_s^4$ . At sufficiently large  $B_c$  or  $B_c^*$  transverse momentum,  $P_T$ , the fragmentation approximation dominates. This process is ideal for quantitatively comparing the fragmentation approximation and the full order  $\alpha_s^4$  calculation, since both can be reliably calculated. We have shown [1] that the fragmentation approximation

\*Presented at the American Physical Society, Division of Particles and Fields Meeting, 10-15 August 1996.

and the full order  $\alpha_s^4$  calculation agree when and only when  $P_T \gg M_{B_c}$ . At small  $P_T$  the non-fragmentation contributions become important since, when the  $B_c$  or  $B_c^*$  is nearly collinear with the initial partons, it is possible for two or more quarks and/or gluons in the subprocesses to simultaneously be nearly on-mass-shell.

## II. CALCULATIONS AND RESULTS

Figure 1 shows the  $P_T$  distributions for the process  $p + \bar{p} \rightarrow B_c(B_c^*) + X$  at the Fermilab Tevatron energy  $\sqrt{s} = 1.8$  TeV with the rapidity cut  $|Y| < 1.5$ . Remarkably, the  $B_c$  meson  $P_T$  distributions agree rather well, even for  $P_T$  as small as about 5 GeV, while for the  $B_c^*$  meson the distributions differ by 50–70% over a much larger range of  $P_T$ , leaving the comparison inconclusive.

The  $P_T$  distributions for the subprocess  $g(k_1) + g(k_2) \rightarrow B_c(P) + b(q_2) + \bar{c}(q_1)$ , which are shown in Fig. 2, are somewhat more revealing. The distributions agree reasonable well when  $P_T$  is larger than about 30 GeV for the  $B_c$  meson and about 40 GeV for the  $B_c^*$  meson. Consequently, the  $P_T$  distributions alone are not decisive and, as will be shown, can even be misleading.

It is more insightful to examine the distributions in  $z = 2(k_1 + k_2) \cdot P/\hat{s}$ , which is simply twice the fraction of the total energy carried by the  $B_c$  or  $B_c^*$  in the subprocess center of mass. Note that  $z$  is experimentally measurable, at least in principle. Figure 3 shows the  $z$  distributions,  $C(z)$ , for the process  $p + \bar{p} \rightarrow B_c(B_c^*) + X$  for  $\sqrt{s} = 1.8$  TeV,  $|Y| < 1.5$ , and  $P_T > 10$  GeV. The distribution [1]  $C(z) \equiv d\sigma/dz$ . From Fig. 3 it is clear that for the  $B_c$  the fragmentation approximation underestimates the full order  $\alpha_s^4$  calculation for small  $z$  and overestimates it for large  $z$ . This results in a cancelation in the  $B_c$   $P_T$  distribution, Fig. 1, fortuitously causing the fragmentation approximation to agree with the full order  $\alpha_s^4$  calculation down to quite small values of  $P_T$ .

However, for the  $B_c^*$  the fragmentation calculation underestimates the full order  $\alpha_s^4$  calculation at all values of  $z$  and no fortuitous cancelation occurs, as for the  $B_c$ .

The relative importance of the fragmentation and non-fragmentation contributions is even more clearly evident in the  $P_T$  distributions for the subprocess  $g + g \rightarrow B_c(B_c^*) + b + \bar{c}$  at very large  $\sqrt{s}$ , as is shown in Fig. 4. Clearly, the non-fragmentation contributions dominate at small  $P_T$ , where two or more quarks and/or gluons can simultaneously be very nearly on-mass-shell in the subprocess.

### III. CONCLUSIONS

We have compared the full order  $\alpha_s^4$  perturbative QCD calculation of the production of  $B_c$  and  $B_c^*$  mesons at the Fermilab Tevatron with the fragmentation approximation. There are Feynman diagrams present in the full order  $\alpha_s^4$  matrix element in which *two or more* quarks and/or gluons can simultaneously be nearly on-mass-shell, and these dominate over the fragmentation approximation at small  $P_T$ . The fragmentation approximation dominates when and only when  $P_T \gg M_{B_c}$ .

### ACKNOWLEDGMENTS

This research was done in collaboration with Chao-Hsi Chang and Yu-Qi Chen and is presented in greater detail in reference 1, where references to previous work can also be found. We acknowledge the support of the U.S. Department of Energy, Division of High Energy Physics, under Grant DE-FG02-91-ER40684 and the National Nature Science Foundation of China.

## REFERENCES

- [1] C.H. Chang, Y.Q. Chen, and R.J. Oakes, Phys. Rev. D, in press.

## FIGURES

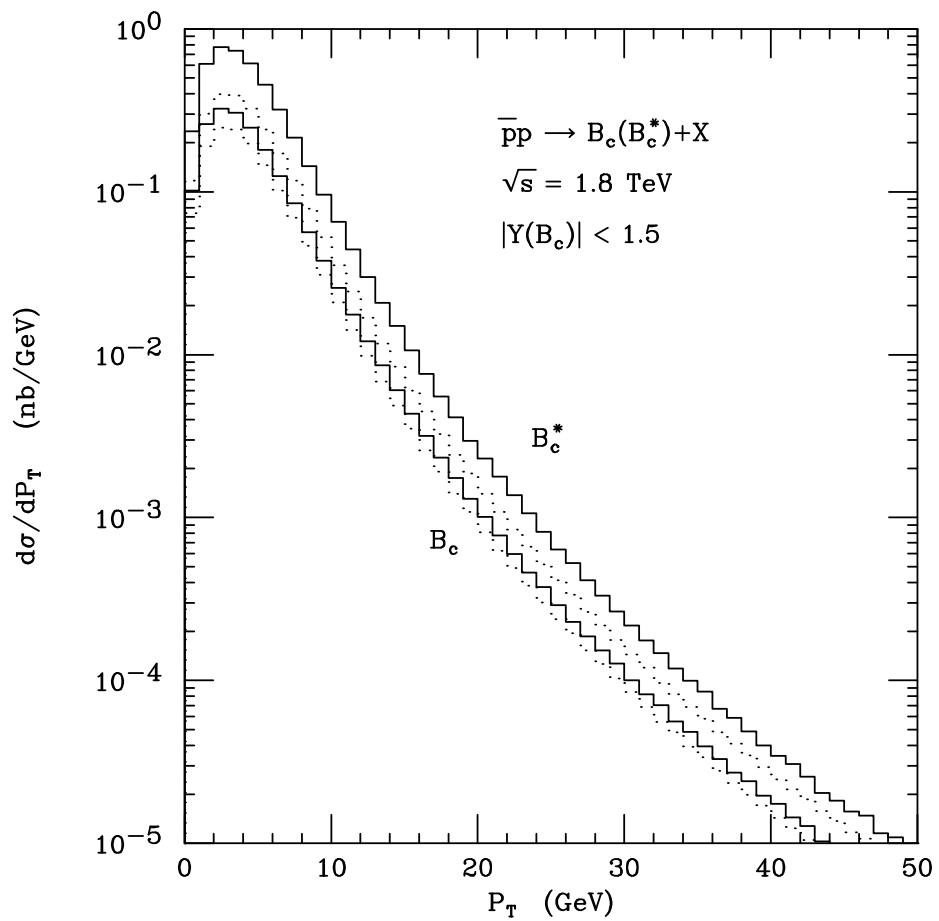


Fig. 1 The  $P_T$  distributions for  $B_c$  and  $B_c^*$  meson production at the Tevatron energy  $\sqrt{s} = 1.8$  TeV. The solid and the dotted lines correspond to the full  $\alpha_s^4$  calculation and the fragmentation approximation, respectively.

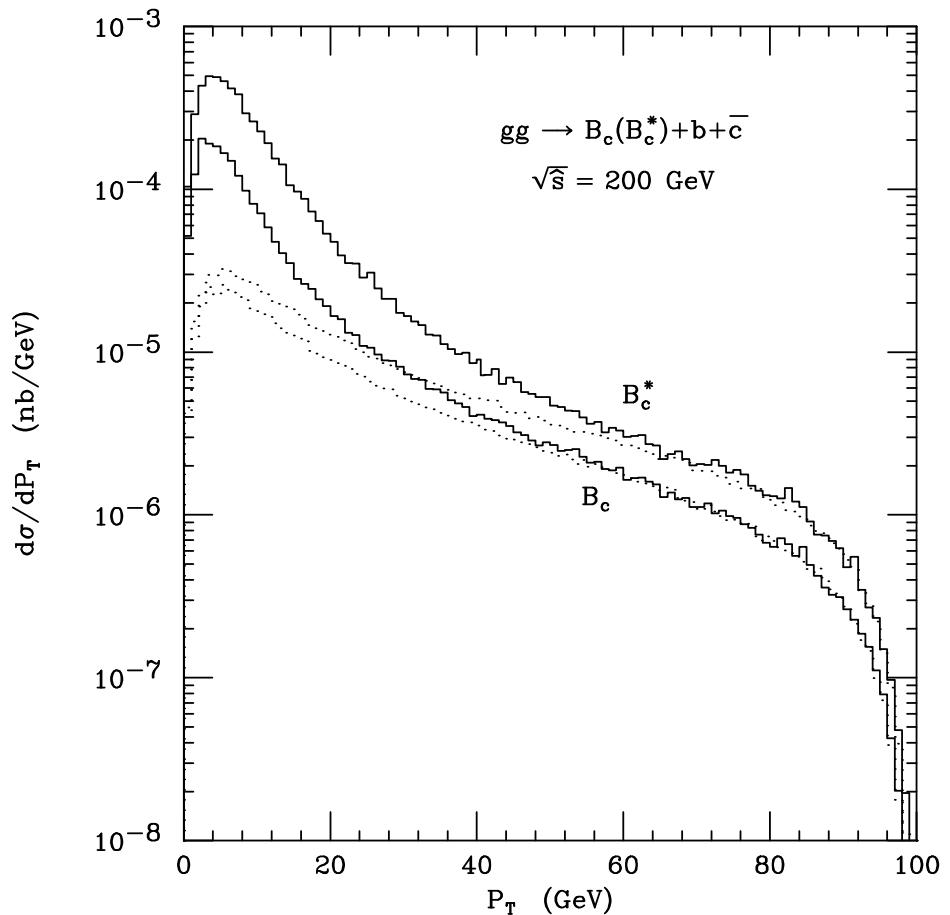


Fig. 2 The  $P_T$  distributions of the  $B_c$  and  $B_c^*$  meson for the subprocess with  $\sqrt{s} = 200$  GeV. The solid and the dotted lines correspond to the full  $\alpha_s^4$  calculation and the fragmentation approximation, respectively.

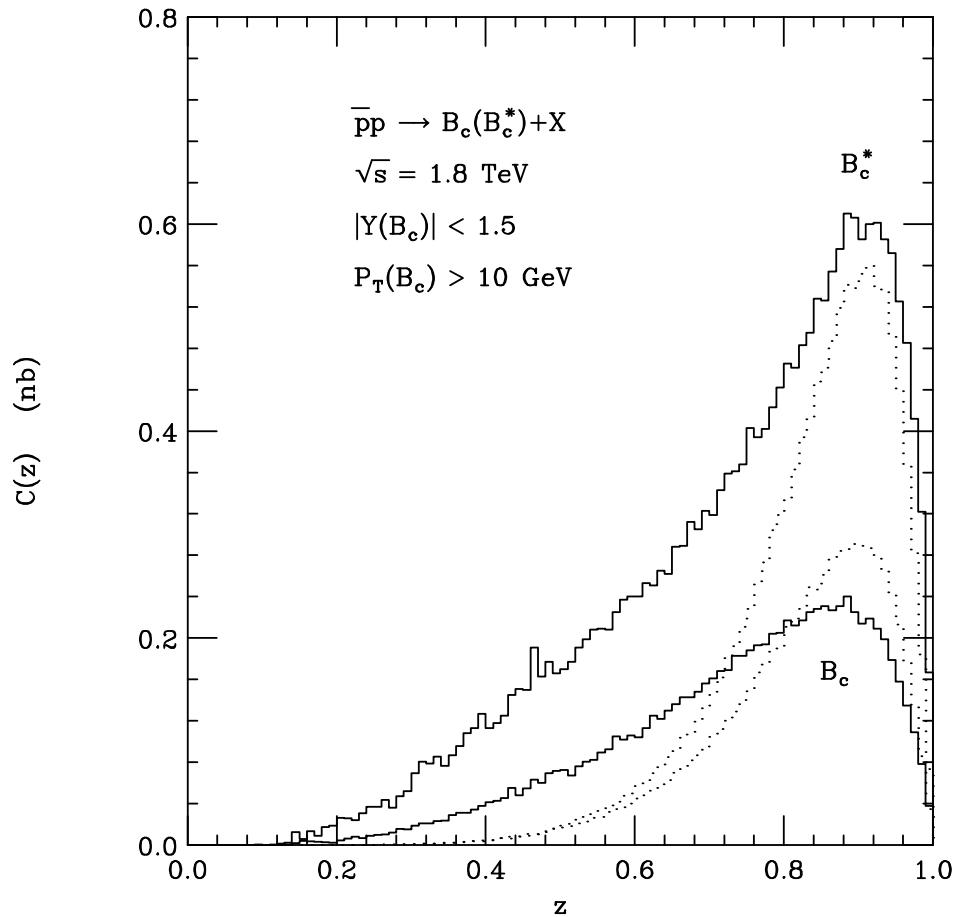


Fig. 3 The  $z$  distributions  $C(z)$  of the  $B_c$  and  $B_c^*$  at the Tevatron energy  $\sqrt{s} = 1.8$  TeV. The solid lines are the full  $\alpha_s^4$  calculation and the dotted lines are the fragmentation approximation with the cut  $P_T > 10$  GeV

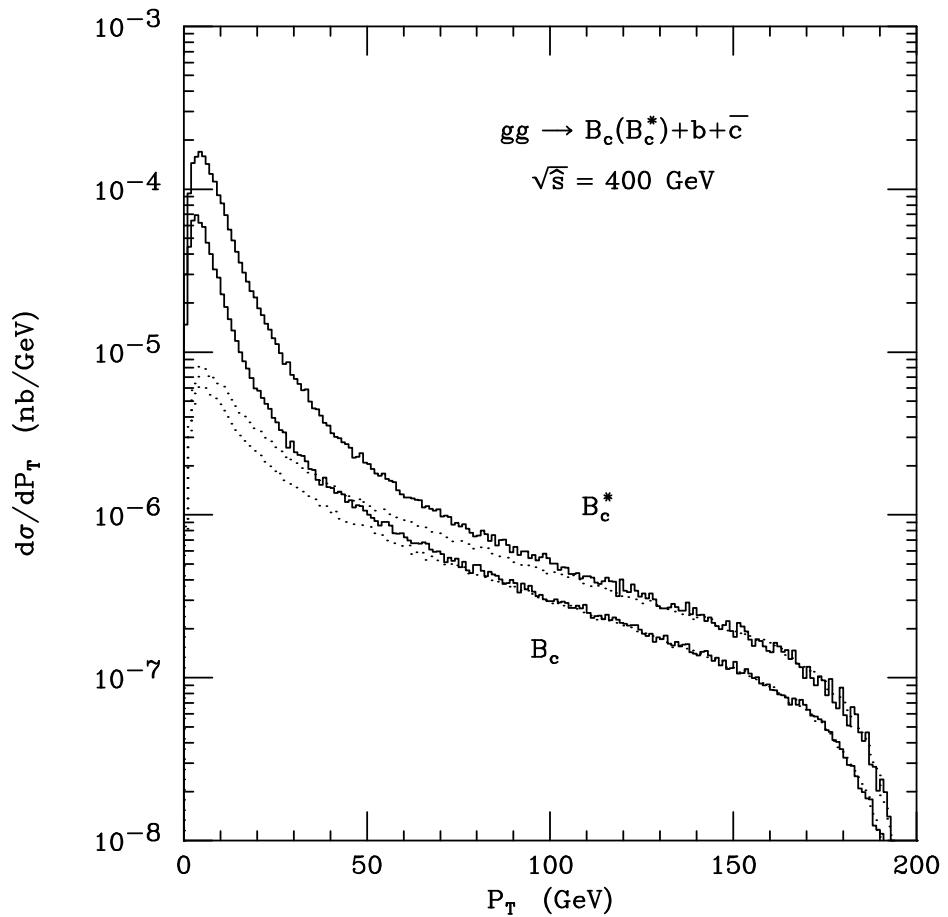


Fig. 4 The  $P_T$  distributions of the  $B_c$  and  $B_c^*$  meson for the subprocess with  $\sqrt{s} = 400 \text{ GeV}$ . The solid and the dotted lines correspond to the full  $\alpha_s^4$  calculation and the fragmentation approximation, respectively.